

1ª Lista de Exercícios de Cálculo I

Equações, Inequações, Módulo ou Valor Absoluto.

Exercício 1 Obtenha o conjunto solução das seguintes equações lineares (equações de 1º grau).

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|-------------------------------|---|--|
| a) $x + 5 = 7$ | b) $5x - 3 = 7$ | c) $12x + 9 = 3$ |
| d) $\sqrt{2} \cdot x - 3 = 2$ | e) $-2x + 8 = 3$ | f) $-8x + 2 = 3$ |
| g) $-\frac{2x}{3} + 8 = 3$ | h) $-\sqrt{5} \cdot x + 8 = 3$ | i) $3x + 9 = 7x - 7$ |
| j) $10x + 3 = 8x + 2$ | k) $5 \cdot (x + 3) + 2x = 3 \cdot (x + 2)$ | l) $2(x - 1) + 3(x - 2) = 4(x - 3)$ |
| m) $3x + 6 = 3 \cdot (x + 2)$ | n) $-3x + 9 = 2(x - 2) - 5x + 13$ | o) $\frac{2}{3} \cdot (3x + 9) = 2x + 6$ |
| p) $3x + 6 = 3 \cdot (x - 2)$ | q) $-3x + 9 = 2(x + 2) - 5x + 13$ | r) $\frac{2}{3} \cdot (3x + 9) = 2x + 5$ |

Resposta:

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|--------------------------------------|-----------------------|--------------------------------------|---|--------------------------------------|--------------------------------------|
| a) $S = \{2\}$ | b) $S = \{2\}$ | c) $S = \left\{-\frac{1}{2}\right\}$ | d) $S = \left\{\frac{5\sqrt{2}}{2}\right\}$ | e) $S = \left\{\frac{5}{2}\right\}$ | f) $S = \left\{-\frac{1}{8}\right\}$ |
| g) $S = \left\{\frac{15}{2}\right\}$ | h) $S = \{\sqrt{5}\}$ | i) $S = \{4\}$ | j) $S = \left\{-\frac{1}{2}\right\}$ | k) $S = \left\{-\frac{9}{4}\right\}$ | l) $S = \{-4\}$ |
| m) $S = \mathbb{R}$ | n) $S = \mathbb{R}$ | o) $S = \mathbb{R}$ | p) $S = \{ \} = \emptyset$ | q) $S = \{ \} = \emptyset$ | r) $S = \{ \} = \emptyset$ |

Exercício 2 Resolva as seguintes inequações lineares.

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|----------------------------------|--|---|
| a) $x + 5 < 7$ | b) $5x - 3 < 7$ | c) $12x + 9 > 3$ |
| d) $\sqrt{2} \cdot x - 3 > 2$ | e) $-2x + 8 < 3$ | f) $-8x + 2 \geq 3$ |
| g) $-\frac{2x}{3} + 8 \leq 3$ | h) $-\sqrt{5} \cdot x + 8 > 3$ | i) $3x + 9 < 7x - 7$ |
| j) $10x + 3 > 8x + 2$ | k) $5 \cdot (x + 3) + 2x \geq 3 \cdot (x + 2)$ | l) $2(x - 1) + 3(x - 2) > 4(x - 3)$ |
| m) $3x + 6 \leq 3 \cdot (x + 2)$ | n) $-3x + 9 > 2(x - 2) - 5x + 13$ | o) $\frac{2}{3} \cdot (3x + 9) \geq 2x + 6$ |
| p) $3x + 6 > 3 \cdot (x - 2)$ | q) $-3x + 9 < 2(x + 2) - 5x + 13$ | r) $\frac{2}{3} \cdot (3x + 9) \geq 2x + 7$ |

Resposta:

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|---|---|---|
| a) $S = \{x \in \mathbb{R}; x < 2\}$ | b) $S = \{x \in \mathbb{R}; x < 2\}$ | c) $S = \{x \in \mathbb{R}; x > -\frac{1}{2}\}$ |
| d) $S = \left\{x \in \mathbb{R}; x > \frac{5\sqrt{2}}{2}\right\}$ | e) $S = \left\{x \in \mathbb{R}; x > \frac{5}{2}\right\}$ | f) $S = \left\{x \in \mathbb{R}; x \leq -\frac{1}{8}\right\}$ |
| g) $S = \left\{x \in \mathbb{R}; x \geq \frac{15}{2}\right\}$ | h) $S = \{x \in \mathbb{R}; x < \sqrt{5}\}$ | i) $S = \{x \in \mathbb{R}; x > 4\}$ |
| j) $S = \left\{x \in \mathbb{R}; x > -\frac{1}{2}\right\}$ | k) $S = \left\{x \in \mathbb{R}; x \geq -\frac{9}{4}\right\}$ | l) $S = \{x \in \mathbb{R}; x > -4\}$ |
| m) $S = \mathbb{R}$ | n) $S = \{ \} = \emptyset$ | o) $S = \mathbb{R}$ |
| p) $S = \mathbb{R}$ | q) $S = \mathbb{R}$ | r) $S = \{ \} = \emptyset$ |

Exercício 3 Resolva as seguintes equações modulares.

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|----------------------------|--|---|
| a) $ x = 5$ | b) $ x = \frac{3}{2}$ | c) $ x = -1$ |
| d) $ x - 3 = 5$ | e) $ x + 8 = 3$ | f) $ x + \frac{2}{3} = 2$ |
| g) $ x - 10 = 8$ | h) $ \pi \cdot \sqrt{3} \cdot \text{sen}(x) \cdot \text{cos}(x) = -100$ | i) $ 2x + 3 = 0$ |
| j) $ \frac{x}{2} - 3 = 5$ | k) $ 5x + 7 = 8$ | l) $ -3x - 2 = 7$ |
| m) $ -3x + 9 = 21$ | n) $ -6x + 2 = 4$ | o) $ \frac{5x}{3} - \frac{2}{4} = \frac{5}{6}$ |

Resposta:

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|---|---|------------------------|---|---|
| a) $S = \{-5, 5\}$ | b) $S = \left\{-\frac{3}{2}, \frac{3}{2}\right\}$ | c) $S = \{ \}$ | d) $S = \{-2, 8\}$ | e) $S = \{-11, -5\}$ |
| f) $S = \left\{-\frac{8}{3}, \frac{4}{3}\right\}$ | g) $S = \{2, 18\}$ | h) $S = \{\emptyset\}$ | i) $S = \left\{-\frac{3}{2}\right\}$ | j) $S = \{-4, 16\}$ |
| k) $S = \left\{-3, \frac{1}{5}\right\}$ | l) $S = \left\{-3, \frac{5}{3}\right\}$ | m) $S = \{-4, 10\}$ | n) $S = \left\{-\frac{1}{3}, 1\right\}$ | o) $S = \left\{-\frac{1}{5}, \frac{4}{5}\right\}$ |

Exercício 4 Resolva as seguintes inequações modulares

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|----------------------|--|--|
| a) $ x < 5$ | b) $ x < 3$ | c) $ x < -1$ |
| d) $ x > 5$ | e) $ x > 3$ | f) $ x > -1$ |
| g) $ x - 10 < 8$ | h) $ \text{sen}(x) \cdot \text{cos}(x) < 0$ | i) $ 2x + 3 \leq 0$ |
| j) $ x - 10 > 8$ | k) $ 5x + 7 \leq 8$ | l) $ -3x - 2 \leq 7$ |
| m) $ 5x + 7 \geq 8$ | n) $ -3x - 2 \geq 7$ | o) $ \frac{5x}{3} - \frac{2}{4} \geq \frac{5}{6}$ |

Resposta:

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|--|--|--|
| S = a) $\{x \in \mathbb{R}; -5 < x < 5\}$ | b) $S = \{x \in \mathbb{R}; -3 < x < 3\}$ | c) $S = \{ \}$ |
| d) $S = \{x \in \mathbb{R}; x < -5 \text{ ou } x > 5\}$ | e) $S = \{x \in \mathbb{R}; x < -3 \text{ ou } x > 3\}$ | f) $S = \mathbb{R}$ |
| g) $S = \{x \in \mathbb{R}; 2 < x < 18\}$ | h) $S = \{ \}$ | i) $S = \left\{-\frac{3}{2}\right\}$ |
| j) $S = \{x \in \mathbb{R}; x < 2 \text{ ou } x > 18\}$ | k) $S = \left\{x \in \mathbb{R}; -3 \leq x \leq \frac{1}{5}\right\}$ | l) $S = \left\{x \in \mathbb{R}; -3 \leq x \leq \frac{5}{3}\right\}$ |
| m) $S = \left\{x \in \mathbb{R}; x \leq -3 \text{ ou } x \geq \frac{1}{5}\right\}$ | n) $S = \left\{x \in \mathbb{R}; x \leq -3 \text{ ou } x \geq \frac{5}{3}\right\}$ | o) $S = \left\{x \in \mathbb{R}; x \leq -\frac{1}{5} \text{ ou } x \geq \frac{4}{5}\right\}$ |